



B⁺/B⁰ Lifetime Ratio

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- B⁺ and B⁰ lifetimes should be the same in naïve spectator model and even down to O(1/m_b²) level
- However there are differences at O(1/m_b³) level explained by Weak Annihilation (for B⁰) and Pauli Interference (for B⁺) diagrams
- In general theory prefers to deal with ratios
- Recent progress in NLO Lattice QCD improved precision of theoretical prediction on the lifetime ratio

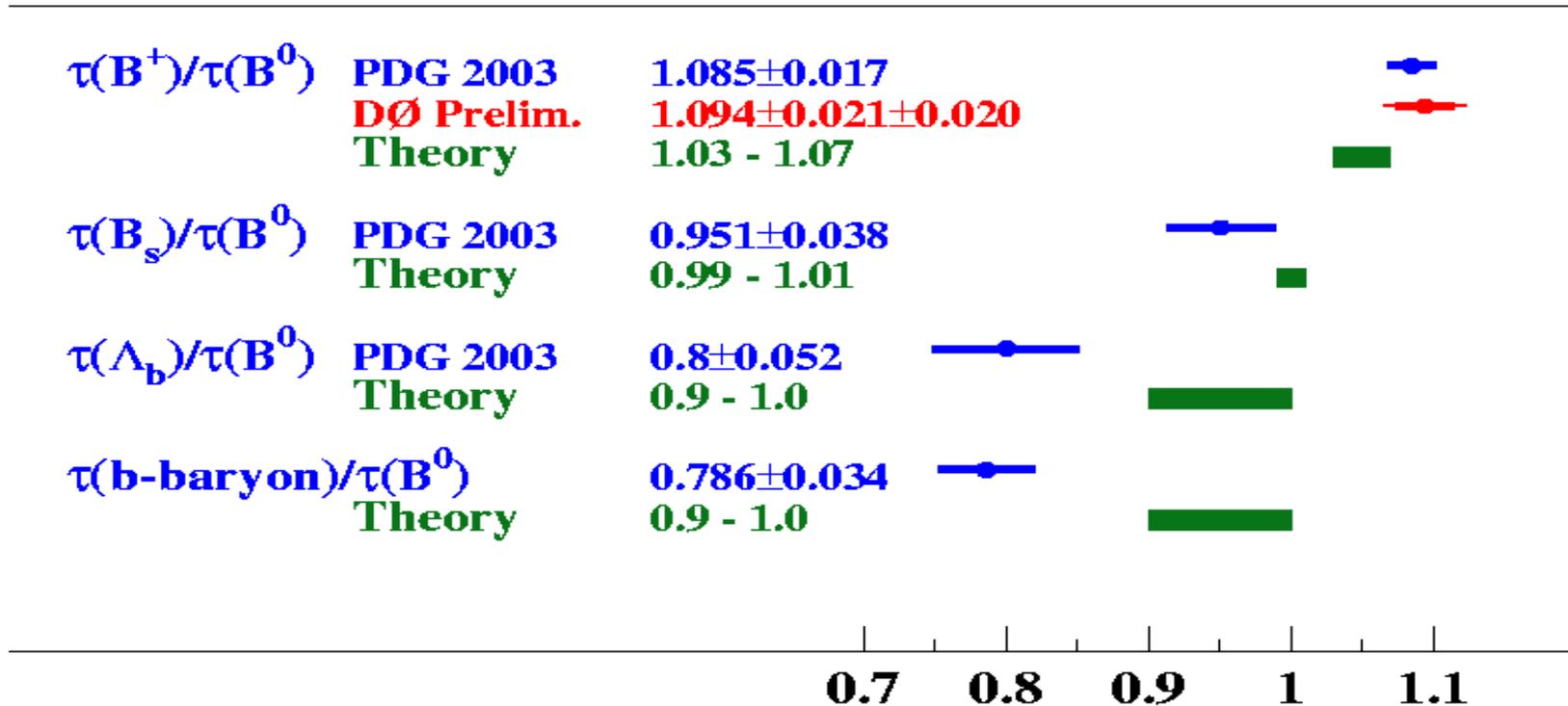
$$\tau(B^+)/\tau(B^0) = 1.053 \pm 0.016 \pm 0.017 (m_B, V_{cb}, f_B)$$

Need improvements in experimental accuracy



Theory Predictions vs Experiment

Lifetime ratio



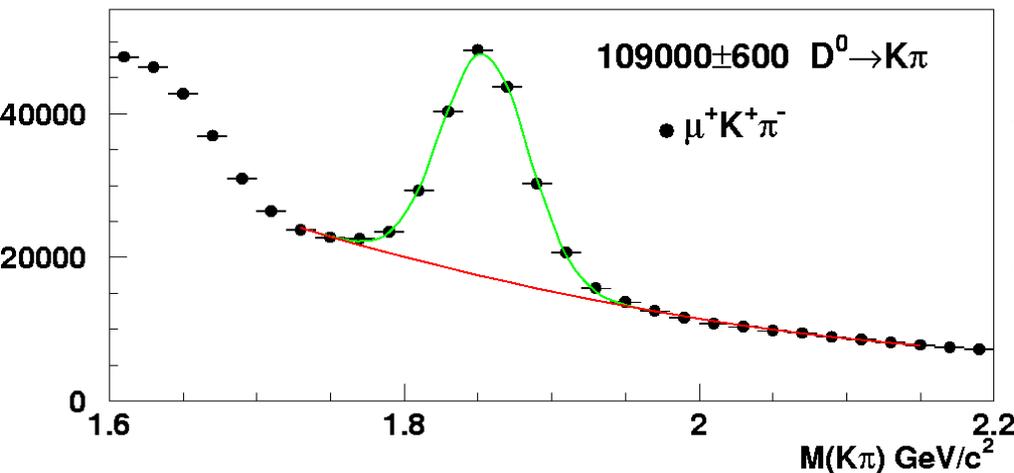


DZero Semileptonic B_d sample

- 109k $B \rightarrow \mu \nu D^0$ candidates
- 25k $B \rightarrow \mu \nu D^*$ candidates

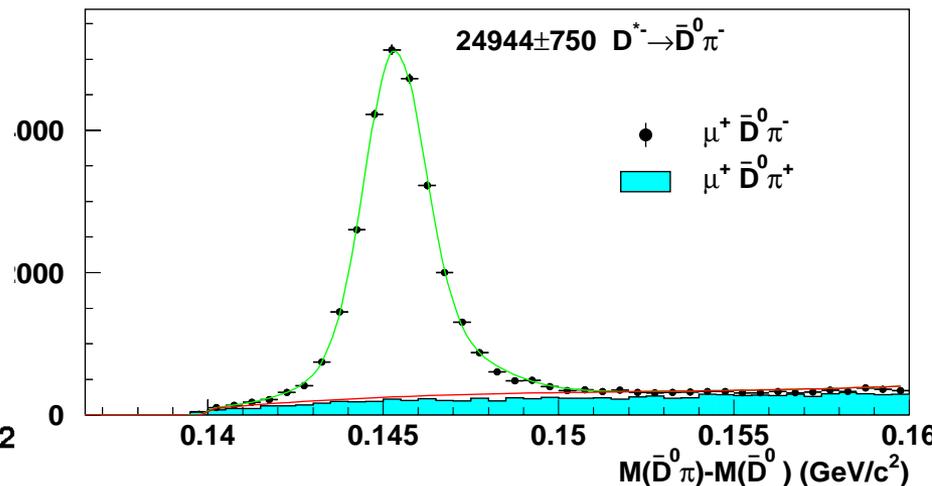


DØ RunII Preliminary, Luminosity=250 pb⁻¹



Dominated by B^+ decays
 B^+ 82% / B^0 16%

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Dominated by B^0 decays
 B^0 86% / B^+ 12%

Above estimates take into account $B \rightarrow \mu \nu \{D, D^*, D^{**}\}$ contributions



Analysis : Novel Technique

Three important points :

1) Measure directly ratio of lifetimes instead of measuring absolute lifetimes

- ◆ Group events into 8 bins of Visible Proper Decay Length (VPDL):

$$\text{VPDL} = L_T / p_T(\mu D^0) \cdot M_B$$

$$L_T = \text{transverse decay length}$$

2) Measure $r = N(\mu D^*)/N(\mu D^0)$ in each bin

- ◆ Number of events is extracted from the fit of mass peak
⇒ no need to know VPDL distribution for background

3) If relative D^*/D^0 efficiency does not depend on VPDL it does not affect the lifetime ratio =>

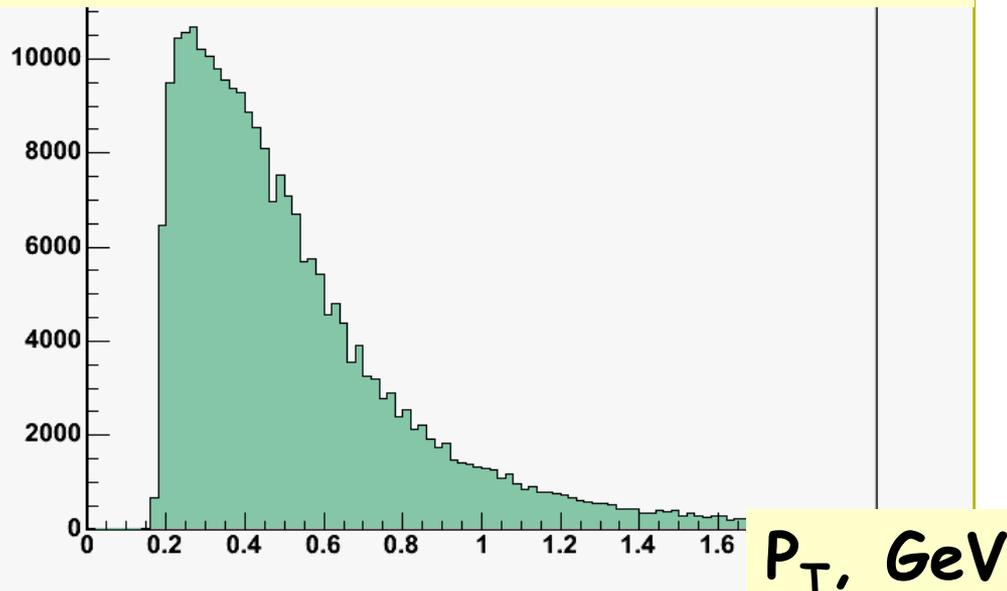
- ◆ Reconstruct slow pion from D^* without biasing lifetime



D* Selections

- Reconstruct slow pion from D* without biasing lifetime
 - ◆ Only requirement on slow pion is to give correct $m(D^*)-m(D^0)$ value
 - ◆ Slow pion is NOT used for calculation of VPDL
 - NOT used in B-vertex
 - NOT used in k-factors

p_T spectrum of soft pion candidate
in $D^* \rightarrow D^0 \pi$





D^0 and D^* Samples

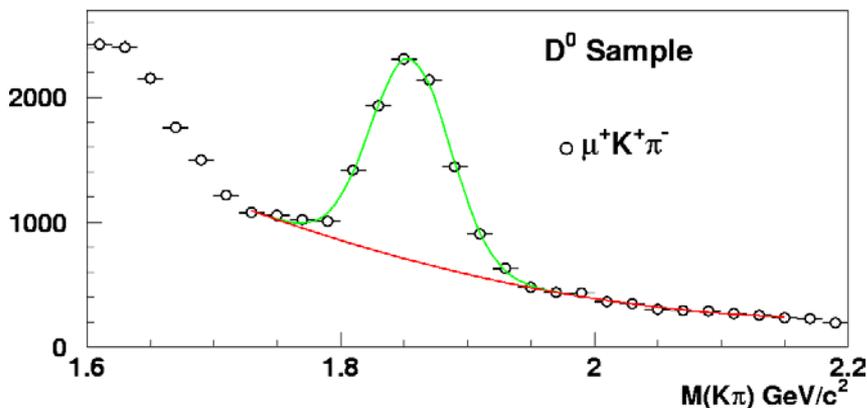
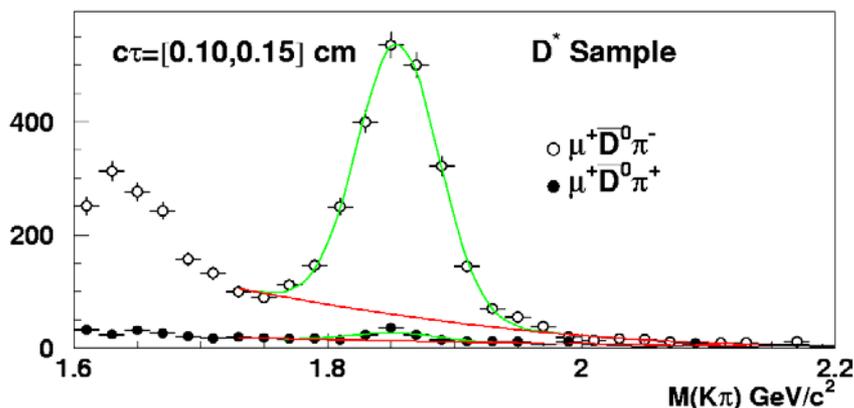
- D^* sample :
 - ◆ all identified D^* candidates
- D^0 sample :
 - ◆ D^0 candidates with removed D^* candidates



Ratio of D^0 and D^* events

one example : VPDL bin [0.10 - 0.15 cm]

DØ RunII Preliminary, Luminosity=250 pb⁻¹



Fit function :
 Gaussian + 2nd order polynomial

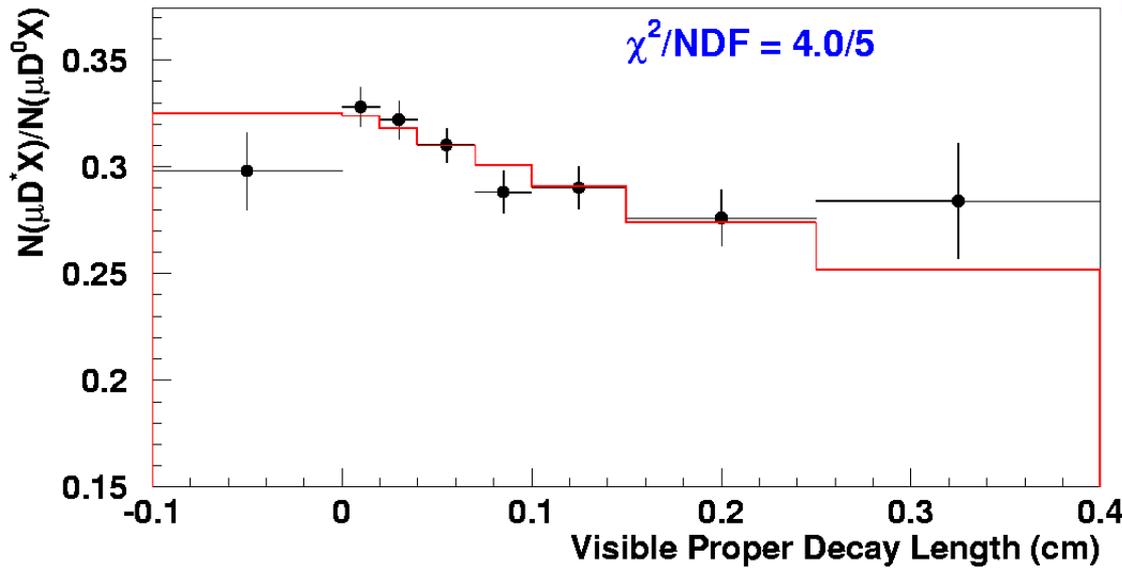
$$r_i = \frac{N_i(\mu^+ D^{*-})}{N_i(\mu^+ \bar{D}^0)} = \frac{N_i^{*R} - C \cdot N_i^{*W}}{N_i^0 + (1 + C) \cdot N_i^{*W}}$$

- Fit D^0 mass peak in both cases in exactly same way
 - Decreases fit systematics
- Number of D^* events is corrected to account for combinatorial bkg
 - Estimated from wrong sign D^* combinations
 - Small correction because D^* S/B is good
- Number of D^0 events is corrected to account for genuine D^0 's lost due to D^* window cut
 - Small correction as well



Measured Ratio vs VPDL

DØ RunII Preliminary, Luminosity = 250 pb⁻¹



Errors are statistical,
derived from the fit of
mass peaks

i	VPDL range	N_i^{*R}	N_i^{*W}	$N_i^0 + N_i^{*W}$	r_i	r_i^e
1	-0.1 ÷ 0.0	1016 ± 39	43 ± 18	3175 ± 109	0.298 ± 0.018	0.325
2	0.0 ÷ 0.02	3482 ± 69	129 ± 22	9973 ± 162	0.328 ± 0.009	0.324
3	0.02 ÷ 0.04	3350 ± 67	111 ± 18	9850 ± 152	0.322 ± 0.009	0.318
4	0.04 ÷ 0.07	3593 ± 70	114 ± 18	10995 ± 155	0.310 ± 0.008	0.310
5	0.07 ÷ 0.10	2175 ± 55	75 ± 13	7144 ± 126	0.288 ± 0.010	0.301
6	0.10 ÷ 0.15	1932 ± 51	57 ± 13	6349 ± 120	0.290 ± 0.010	0.291
7	0.15 ÷ 0.25	1212 ± 42	36 ± 11	4189 ± 102	0.276 ± 0.013	0.274
8	0.25 ÷ 0.40	298 ± 21	5 ± 6	1022 ± 51	0.284 ± 0.027	0.252



Fitting Procedure

$k \equiv \tau^+ / \tau^0 - 1$ is determined from $\chi^2(N, k)$ minimisation:

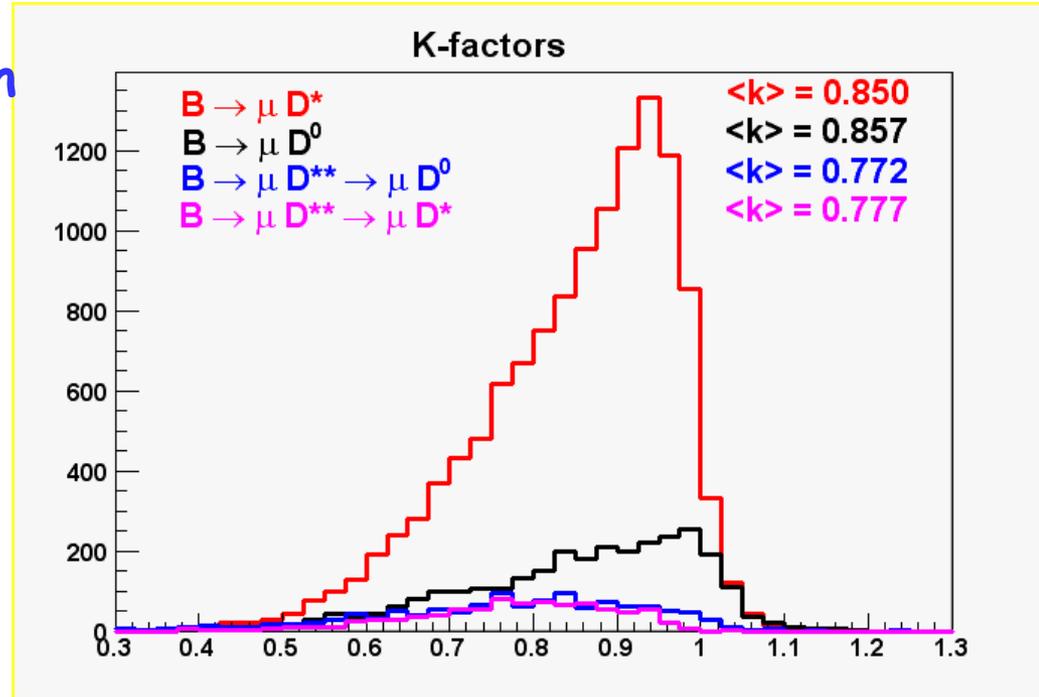
$$\chi^2(N, k) = \sum_i \frac{(r_i - N \cdot r_i^e(k))^2}{\sigma^2(r_i)}$$

- Norm N and k are free parameters in minimisation;
- $\tau^+ = 1.674 \pm 0.018$ ps is taken from PDG;
- $\tau^0 = \tau^+ / (1 + k)$;
- Br_j are taken from PDG;
- $D_j(K)$, $Res_j(x)$ are taken from simulation;
- $Eff_{D^0}(x)$ is taken from simulation;
- $Eff_{D^*}(x) = C \cdot Eff_{D^0}(x)$ - verified in simulation;



K-factors

- K-factor accounts for missing decay products like neutrino in calculation of proper lifetime
- Production $B \rightarrow D^{*(0,+)} \mu \nu X$ dominates both D^0 and D^* samples
- We always compute k -factors as :
$$= P_T(\mu D^0) / P_T(B)$$
 even for D^{*+} sample
- Same K-factor for D^{*+} and D^{*0}
- Reduce systematic error
- K-factors are grouped into 4 categories

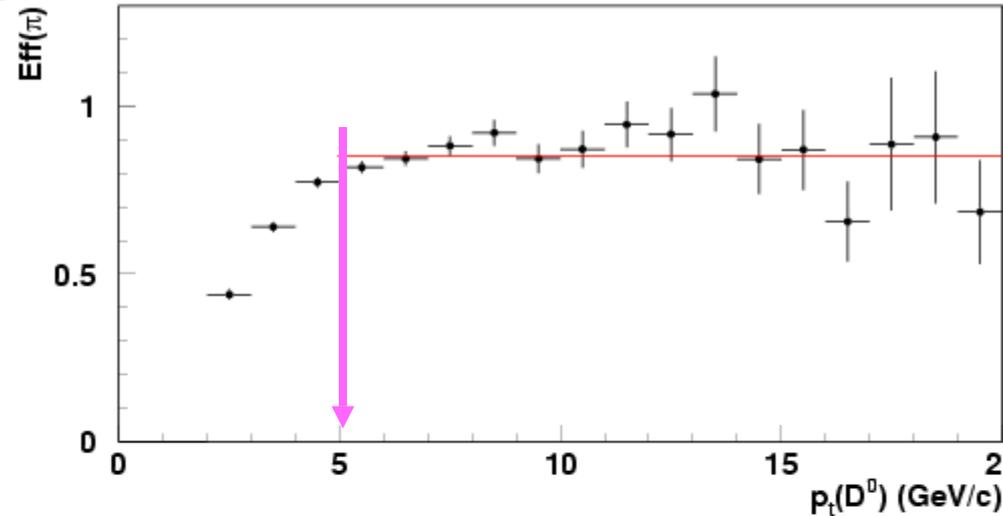




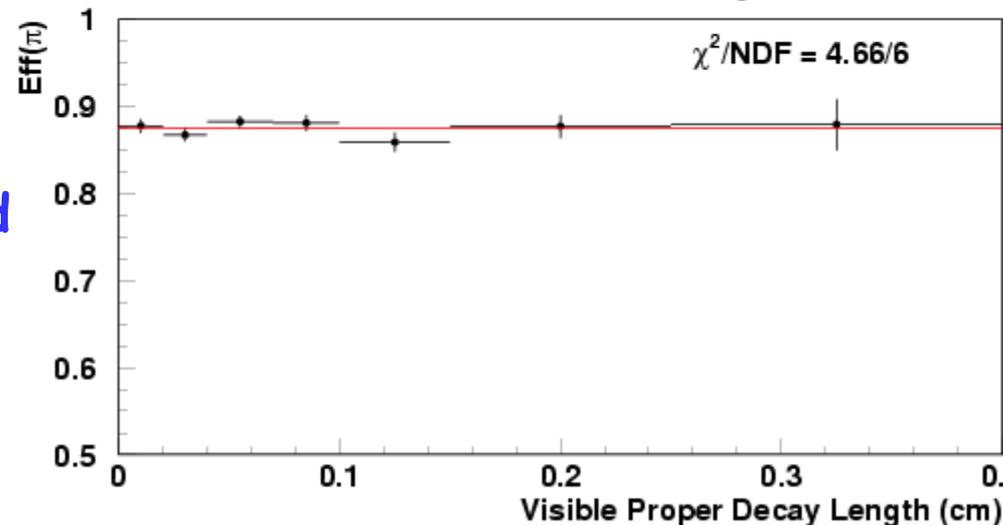
Slow pion efficiency

DØ RunII Preliminary

- Key point : Want to avoid lifetime bias
- Eff depends on $P_T(D^0)$ because of tracking cutoff at $P_T=0.183$ GeV
 - ◆ May induce VPDL dependence
 - ◆ Cut at 5 GeV
 - ▲ Removes 35% of events
 - ▲ Should help to remove $c\bar{c}$ and $B \rightarrow D_s D$ contributions
- After that Eff = 88% and does not depend on VPDL in MC
- Error on possible slope was used to estimate systematics
- Investigating ways to double check it in data



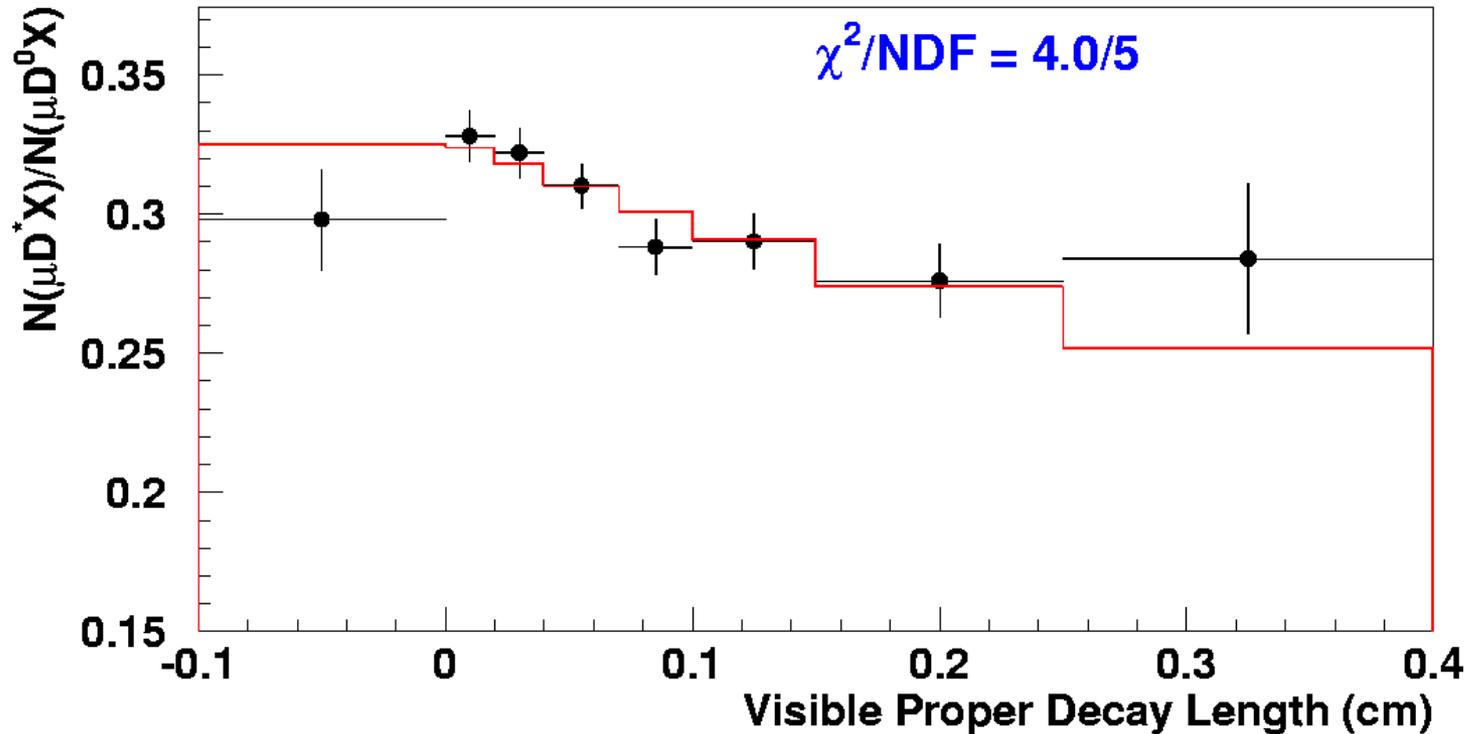
DØ RunII Preliminary





$\tau(B^+)/\tau(B^0)$: Result

DØ RunII Preliminary, Luminosity = 250 pb⁻¹



Preliminary result:

$$\tau(B^+)/\tau(B^0) = 1.093 \pm 0.021 \text{ (stat)} \pm 0.022 \text{ (syst)}$$

$$N = 1.001 \pm 0.012$$



Systematic errors

source	variation range	$\Delta(\tau^+/\tau^0)$
$Br(B_d^0 \rightarrow \mu^+ \nu D^{*-})$	$5.53 \pm 0.23\%$	0.0015
$Br(B^+ \rightarrow \mu^+ \nu \bar{D}^{*0})$	$6.50 \pm 0.5\%$	0.0001
$Br(B^+ \rightarrow \mu^+ \nu \bar{D}^{**0})$	$2.67 \pm 0.37\%$	0.0005
$Br(B^+ \rightarrow \mu^+ \nu D^{*-} \pi^+ X)$	$1.06 \pm 0.25\%$	0.0074
$Br(B_s^0 \rightarrow \mu^+ \nu D_s X)$	$7.9 \pm 2.4\%$	0.0025
R_s^{**} , see (11)	$0 \div 1$	0.0007
$Eff(x; B^+ \rightarrow \mu^+ \nu D^{*0})$	set $Eff(x) = const$	0.0012
$Eff(\pi)$	0.876 ± 0.04	0.0012
Time dependence of $Eff(x; \pi)$	slope ± 0.12 [1/cm]	0.0132
C_Y	$C_Y = 1$	0.0086
VPDL resolution	MC resolution $\times (0.2 \div 4.0)$	0.0042
difference in resolution between D^* and D^0	$r_1^e \rightarrow r_1$	0.0060
K -factors	average value $\pm 2\%$	0.0021
K -factors	$Z(K; D^{**}) = Z(K; D^0, D^*)$	0.0072
Fitting procedure	see section 10	0.0060
C from eqn. (2)	1.22 ± 0.04	0.0004
Total		0.0215

- Work in progress to understand (and hopefully decrease) main contributors



Consistency Checks

- Split data sample in two parts wrt various parameters - all looks good

Consistency test	k
$ Z_{PV} < 15\text{cm}$	0.099 ± 0.028
$ Z_{PV} > 15\text{cm}$	0.091 ± 0.031
$\eta(\text{muon}) > 0$	0.107 ± 0.031
$\eta(\text{muon}) < 0$	0.079 ± 0.030
$p_T(\text{D}^0) < 7.5 \text{ GeV}/c$	0.105 ± 0.031
$p_T(\text{D}^0) > 7.5 \text{ GeV}/c$	0.083 ± 0.030
μ^+ only	0.088 ± 0.030
μ^- only	0.111 ± 0.031
$p_T(\mu) < 5.5 \text{ GeV}/c$	0.104 ± 0.033
$p_T(\mu) > 5.5 \text{ GeV}/c$	0.083 ± 0.028
Different intervals	0.086 ± 0.021
Without last VPDL interval	0.107 ± 0.024
Additional VPDL interval 0.4-0.8 cm	0.092 ± 0.021

- Measured ratio in MC = 0.073 ± 0.030 (input 0.070)



Summary

- Performed precise measurement of B^+/B^0 lifetime ratio
 - ◆ Competitive with B-factories

Preliminary result:

$$\tau(B^+)/\tau(B^0) = 1.093 \pm 0.021 \text{ (stat)} \pm 0.022 \text{ (syst)}$$

- Working on final systematic errors
- Statistics is flowing in
 - ◆ Proposal to increase L3 BW and write more B-mesons on tape is on the table